

Calcola le seguenti derivate:

$$y = \frac{2}{x\sqrt{x}-2} = \frac{1}{x^{\frac{3}{2}}-2}$$

$$y' = \frac{-2 \cdot \frac{3}{2} x^{\frac{1}{2}}}{\left(x^{\frac{3}{2}}-2\right)^2} = -\frac{3\sqrt{x}}{(x\sqrt{x}-2)^2}$$

$$y = \frac{e^x(x+1)}{x^2} = e^x \left(\frac{1}{x} + \frac{1}{x^2} \right)$$

$$y' = e^x \left(\frac{1}{x} + \frac{1}{x^2} \right) + e^x \left(-\frac{1}{x^2} - \frac{2}{x^3} \right) = e^x \left(\frac{1}{x} + \frac{1}{x^2} - \frac{1}{x^2} - \frac{2}{x^3} \right) = e^x \frac{x^2-2}{x^3}$$

$$y = \sin x \cot x = \sin x \frac{\cos x}{\sin x} = \cos x$$

$$y' = -\sin x$$

$$y = 2\sqrt[3]{x} + \sqrt[3]{x^2} + \frac{1}{\sqrt[3]{x^2}} + \frac{2}{\sqrt[3]{x}} = 2x^{\frac{1}{3}} + x^{\frac{2}{3}} + x^{-\frac{2}{3}} + 2x^{-\frac{1}{3}}$$

$$y' = 2 \cdot \frac{1}{3} x^{-\frac{2}{3}} + \frac{2}{3} x^{-\frac{1}{3}} - \frac{2}{3} x^{-\frac{5}{3}} - \frac{2}{3} x^{-\frac{4}{3}} = \frac{2}{3\sqrt[3]{x^2}} + \frac{2}{3\sqrt[3]{x}} - \frac{2}{3x\sqrt[3]{x^2}} - \frac{2}{3x\sqrt[3]{x}} = 2 \cdot \frac{x + x\sqrt[3]{x} - 1 - \sqrt[3]{x}}{3x\sqrt[3]{x^2}} = \frac{2(x-1)(1+\sqrt[3]{x})}{3x\sqrt[3]{x^2}}$$

$$y = \frac{x + \sqrt{x}}{\sqrt{x}} = \sqrt{x} + 1$$

$$y' = \frac{1}{2\sqrt{x}}$$

$$y = \frac{3x+2}{4x} = \frac{3}{4} + \frac{1}{2x}$$

$$y' = -\frac{1}{2x^2}$$

$$y = \frac{1}{x} + 2 \ln x + \frac{\ln x}{x}$$

$$y' = -\frac{1}{x^2} + \frac{2}{x} + \frac{1}{x^2} - \frac{\ln x}{x^2} = \frac{2}{x} - \frac{\ln x}{x^2} = \frac{2x - \ln x}{x^2}$$

$$y = \frac{x-1}{x+1}$$

$$y' = \frac{x+1-(x-1)}{(x+1)^2} = \frac{x+1-x+1}{(x+1)^2} = \frac{2}{(x+1)^2}$$

$$y = \frac{4}{x-2}$$

$$y' = -\frac{4}{(x-2)^2}$$

$$y = \frac{1 + \sin x}{1 - \cos x}$$

$$y' = \frac{\cos x (1 - \cos x) - \sin x (1 + \sin x)}{(1 - \cos x)^2} = \frac{\cos x - \cos^2 x - \sin x - \sin^2 x}{(1 - \cos x)^2} = \frac{\cos x - \sin x - 1}{(1 - \cos x)^2}$$