

$$1. \int \left(\frac{1}{\sqrt[3]{x^2}} - \frac{5}{x^3} + \sqrt[5]{x} \right) dx$$

$$\int x^{-\frac{2}{3}} dx - 5 \int x^{-3} dx + \int x^{\frac{1}{5}} dx = 3x^{\frac{1}{3}} - \frac{5}{-2}x^{-2} + \frac{5}{6}x^{\frac{6}{5}} + c = 3\sqrt[3]{x} + \frac{5}{2x^2} + \frac{5}{6}x\sqrt[5]{x} + c$$

$$2. \int \frac{2 + x^2 - x^4}{x^2} dx$$

$$\int \left(\frac{2}{x^2} + 1 - x^2 \right) dx = 2 \int x^{-2} dx + \int 1 dx - \int x^2 dx = \frac{2}{-1} x^{-1} + x - \frac{x^3}{3} + c = -\frac{2}{x} + x - \frac{x^3}{3} + c$$

$$3. \int \frac{\sqrt{x} + 4}{x} dx$$

$$\int \frac{1}{\sqrt{x}} dx + 4 \int \frac{1}{x} dx = 2\sqrt{x} + 4 \ln |x| + c$$

$$4. \int \frac{x^3 + 6x^2 + 12x + 8}{2 + x} dx$$

$$\int \frac{(x+2)^3}{x+2} dx = \int (x+2)^2 dx = \frac{(x+2)^3}{3} + c$$

$$5. \int \frac{2 - \operatorname{sen}^2 x}{\cos^2 x} dx$$

$$\int \frac{1 + 1 - \operatorname{sen}^2 x}{\cos^2 x} dx = \int \frac{1 + \cos^2 x}{\cos^2 x} dx = \int \left(\frac{1}{\cos^2 x} + 1 \right) dx = \operatorname{tg} x + x + c$$

$$6. \int (\operatorname{tg}^2 x - \operatorname{ctg}^2 x) dx$$

$$\int (\operatorname{tg}^2 x + 1 - \operatorname{ctg}^2 x - 1) dx = \operatorname{tg} x + \operatorname{ctg} x + c$$

$$7. \int e^{x+2} dx$$

$$= e^{x+2} + c$$

$$8. \int \frac{\arctan x}{1+x^2} dx$$

$$t = \arctan x \quad dt = \frac{1}{1+x^2} dx \quad \int t dt = \frac{t^2}{2} + c = \frac{(\arctan x)^2}{2} + c$$

$$9. \int \frac{2x^3 + 1}{\sqrt{x^4 + 2x}} dx$$

$$\frac{1}{2} \int \frac{4x^3 + 2}{\sqrt{x^4 + 2x}} dx = \frac{1}{2} \cdot 2 (x^4 + 2x)^{\frac{1}{2}} = \sqrt{x^4 + 2x} + c$$

$$10. \int \frac{2x-1}{4x^2+4} dx$$

$$\frac{1}{4} \int \frac{2x-1}{x^2+1} dx = \frac{1}{4} \int \frac{2x}{x^2+1} dx - \frac{1}{4} \int \frac{1}{1+x^2} dx = \frac{1}{4} \ln(x^2+1) - \frac{1}{4} \arctan x + c$$

$$11. \int \frac{e^x + 1}{e^x + x} dx$$

$$D(e^x + x) = e^x + 1 \quad = \ln |e^x + x| + c$$

$$12. \int \frac{1}{\sqrt{x}} 2^{\sqrt{x}} dx$$

$$t = \sqrt{x} \quad dt = \frac{1}{2\sqrt{x}} dx \quad 2 \int 2^t dt = \frac{2}{\ln 2} 2^t + c = \frac{2}{\ln 2} 2^{\sqrt{x}} + c$$

$$13. \int \frac{1}{x(1+\ln^2 x)} dx$$

$$t = \ln x \quad dt = \frac{1}{x} dx \quad \int \frac{1}{1+t^2} dt = \arctan t + c = \arctan \ln x + c$$

$$14. \int \frac{2x^3 + 4x + 1}{2x + 3} dx$$

$$\begin{array}{r|l}
 \begin{array}{r}
 2x^3 \quad 4x \quad +1 \\
 -2x^3 \quad -3x^2 \\
 \hline
 -3x^2 \quad 4x \quad +1 \\
 +3x^2 \quad +\frac{9}{2}x \\
 \hline
 \frac{17}{2}x \quad +1 \\
 -\frac{17}{2}x \quad -\frac{51}{4} \\
 \hline
 \frac{47}{4} \\
 -\frac{47}{4} \\
 \hline
 \end{array} & \begin{array}{l}
 2x + 3 \\
 \hline
 x^2 - \frac{3}{2}x + \frac{17}{4}
 \end{array}
 \end{array}$$

$$\begin{aligned}
 & \int \left(x^2 - \frac{3}{2}x + \frac{17}{4} - \frac{47}{4} \cdot \frac{1}{2x+3} \right) dx = \\
 & = \int x^2 dx - \frac{3}{2} \int x dx + \frac{17}{4} \int 1 dx - \frac{47}{8} \int \frac{2}{2x+3} dx = \\
 & = \frac{x^3}{3} - \frac{3}{4}x^2 + \frac{17}{4}x - \frac{47}{8} \ln|2x+3| + c
 \end{aligned}$$

$$15. \int \frac{x+4}{4x^2+12x+9} dx$$

$$\begin{aligned}
 & \frac{1}{2} \int \frac{2x+8}{(2x+3)^2} dx = \frac{1}{2} \int \left(\frac{2x+3}{(2x+3)^2} + \frac{5}{(2x+3)^2} \right) dx = \\
 & = \frac{1}{4} \int \frac{2}{2x+3} dx + \frac{5}{4} \int \frac{2}{(2x+3)^2} dx = \frac{1}{4} \ln|2x+3| - \frac{5}{4(2x+3)} + c
 \end{aligned}$$

$$16. \int \frac{2x}{x^2+2x+2} dx$$

$$\int \frac{2x+2-2}{x^2+2x+2} dx = \int \left(\frac{2x+2}{x^2+2x+2} - \frac{2}{(x+1)^2+1} \right) dx = \ln|x^2+2x+2| - 2 \operatorname{arctg}(x+1) + c$$

$$17. \int \frac{dx}{e^x + e^{-x}}$$

$$\int \frac{dx}{e^x + \frac{1}{e^x}} = \int \frac{e^x}{1 + e^{2x}} dx = \operatorname{arctg} e^x + c$$

$$18. \int \frac{x^3}{e^{x^2}} dx$$

$$\int x^3 e^{-x^2} dx = \frac{1}{2} \int x^2 \cdot 2x e^{-x^2} dx$$

$$\begin{array}{ll}
 f(x) = x^2 & f'(x) = 2x \\
 g'(x) = 2x e^{-x^2} & g(x) = -e^{-x^2}
 \end{array}$$

$$= -\frac{1}{2} x^2 e^{-x^2} + \int x e^{-x^2} dx = -\frac{1}{2} x^2 e^{-x^2} - \frac{1}{2} e^{-x^2} + c = -\frac{x^2 + 1}{2e^{x^2}} + c$$