

$$1. \frac{a^3+3a^2+3a+1}{a^2+2a+1} \cdot \frac{2a-2}{1-a^2}$$

$$= \frac{(a+1)^3}{(a+1)^2} \cdot \frac{2(a-1)}{-(a-1)(a+1)} = -2$$

$$C.E.: a \neq \pm 1$$

$$2. \left[\left(\frac{a}{a^2-a-6} + \frac{1}{a^2-9} \right) \cdot \frac{a-3}{a^2+4a+2} + \frac{1}{a+3} \right] (4a+8)$$

$$= \left[\left(\frac{a}{(a-3)(a+2)} + \frac{1}{(a-3)(a+3)} \right) \cdot \frac{a-3}{a^2+4a+2} + \frac{1}{a+3} \right] 4(a+2) =$$

$$C.E.: \begin{cases} a \neq \pm 3 \\ a \neq -2 \\ a^2 + 4a + 2 \neq 0 \end{cases}$$

$$= \left[\frac{a(a+3)+a+2}{(a-3)(a+3)(a+2)} \cdot \frac{a-3}{a^2+4a+2} + \frac{1}{a+3} \right] 4(a+2) =$$

$$= \left(\frac{a^2+4a+2}{(a-3)(a+3)(a+2)} \cdot \frac{a-3}{a^2+4a+2} + \frac{1}{a+3} \right) 4(a+2) =$$

$$= \left(\frac{1}{(a+3)(a+2)} + \frac{1}{a+3} \right) 4(a+2) = \frac{1+a+2}{(a+3)(a+2)} \cdot 4(a+2) = \frac{a+3}{(a+3)(a+2)} \cdot 4(a+2) = 4$$

$$3. \left(\frac{x-3}{3x-3} - \frac{1}{1-x^2} \right) \left(\frac{1}{x} + 2 + x \right) \cdot \frac{3}{x-2} \cdot (x-1) - x - 9$$

$$= \left(\frac{x-3}{3(x-1)} - \frac{1}{-(x-1)(x+1)} \right) \left(\frac{1+2x+x^2}{x} \right) \cdot \frac{3}{x-2} \cdot (x-1) - x - 9 =$$

$$C.E.: \begin{cases} x \neq 0 \\ x \neq \pm 1 \\ x \neq 2 \end{cases}$$

$$= \frac{(x-3)(x+1)+3}{3(x-1)(x+1)} \cdot \frac{(x+1)^2}{x} \cdot \frac{3}{x-2} \cdot (x-1) - x - 9 =$$

$$= \frac{x^2-3x+x-3+3}{x(x-2)} \cdot (x+1) - x - 9 =$$

$$= \frac{x^2-2x}{x(x-2)} \cdot (x+1) - x - 9 = \frac{x(x-2)}{x(x-2)} \cdot (x+1) - x - 9 = x+1-x-9 = -8$$

$$4. \frac{(16a-32)(a^2-1)}{a^3-1} \left(\frac{1}{2a^2-3a-2} - \frac{1}{a^3+a^2-4a-4} \right) (2a^2 + 5a + 2)$$

$$= \frac{16(a-2)(a+1)(a-1)}{(a-1)(a^2+a+1)} \left(\frac{1}{2a^2-4a+a-2} - \frac{1}{a^2(a+1)-4(a+1)} \right) (2a^2+4a+a+2) =$$

$$C.E.: \begin{cases} a \neq \pm 1 \\ a \neq \pm 2 \\ a \neq -\frac{1}{2} \end{cases}$$

$$= \frac{16(a-2)(a+1)}{a^2+a+1} \left(\frac{1}{2a(a-2)+(a-2)} - \frac{1}{(a+1)(a^2-4)} \right) [2a(a+2)+1(a+2)] =$$

$$= \frac{16(a-2)(a+1)}{a^2+a+1} \left(\frac{1}{(a-2)(2a+1)} - \frac{1}{(a+1)(a-2)(a+2)} \right) (a+2)(2a+1) =$$

$$= \frac{16(a-2)(a+1)}{a^2+a+1} \cdot \frac{(a+1)(a+2) - (2a+1)}{(2a+1)(a-2)(a+2)(a+1)} \cdot (a+2)(2a+1) =$$

$$= \frac{16}{a^2+a+1} \cdot (a^2+2a+a+2-2a-1) = \frac{16}{a^2+a+1} \cdot (a^2+a+1) = \mathbf{16}$$