

Equazioni logaritmiche

1. $\log_{\frac{1}{3}} x = -3$

$$x = \left(\frac{1}{3}\right)^3 \Rightarrow x = 27$$

2. $\log_4 x = 2$

$$x = 4^2 \Rightarrow x = 16$$

3. $\log_{\frac{1}{4}} x = \frac{3}{2}$

$$x = \left(\frac{1}{4}\right)^{\frac{3}{2}} \Rightarrow x = \left[\left(\frac{1}{2}\right)^2\right]^{\frac{3}{2}} \Rightarrow x = \left(\frac{1}{2}\right)^3 \Rightarrow x = \frac{1}{8}$$

4. $\log x = 0,01$

$$x = 10^{0,01} \Rightarrow x = \sqrt[100]{10}$$

5. $\log_{\frac{2}{3}} x = 1$

$$x = \left(\frac{2}{3}\right)^1 \Rightarrow x = \frac{2}{3}$$

6. $\log_{\frac{2}{5}} x = -\frac{3}{4}$

$$x = \left(\frac{2}{5}\right)^{-\frac{3}{4}} \Rightarrow x = \left(\frac{5}{2}\right)^{\frac{3}{4}} \Rightarrow x = \sqrt[4]{\left(\frac{5}{2}\right)^3}$$

7. $\log_{\frac{3}{8}} x = -2$

$$x = \left(\frac{3}{8}\right)^{-2} \Rightarrow x = \left(\frac{8}{3}\right)^2 \Rightarrow x = \frac{64}{9}$$

8. $\log_{\frac{8}{27}} x = -\frac{1}{3}$

$$x = \left(\frac{8}{27}\right)^{-\frac{1}{3}} \Rightarrow x = \left[\left(\frac{2}{3}\right)^3\right]^{-\frac{1}{3}} \Rightarrow x = \left(\frac{2}{3}\right)^{-1} \Rightarrow x = \frac{3}{2}$$

Equazioni logaritmiche

9. $\log_{\sqrt{2}} x = -2$

$$x = (\sqrt{2})^{-2} \Rightarrow x = \left(\frac{1}{\sqrt{2}}\right)^2 \Rightarrow x = \frac{1}{2}$$

10. $\log_{25} x = \frac{1}{2}$

$$x = 25^{\frac{1}{2}} \Rightarrow x = 5$$

11. $\log_{\frac{3}{4}} x = -\frac{3}{4}$

$$x = \left(\frac{3}{4}\right)^{-\frac{3}{4}} \Rightarrow x = \left(\frac{4}{3}\right)^{\frac{3}{4}} \Rightarrow x = \sqrt[4]{\frac{64}{27}}$$

12. $\log_{\sqrt[4]{3}} x = 4$

$$x = (\sqrt[4]{3})^4 \Rightarrow x = [(3)^{\frac{1}{4}}]^4 \Rightarrow x = 3$$

13. $\log_{\frac{1}{2}} x = -\frac{2}{3}$

$$x = \left(\frac{1}{2}\right)^{-\frac{2}{3}} \Rightarrow x = 2^{\frac{2}{3}} \Rightarrow x = \sqrt[3]{4}$$

14. $\log_{\frac{4}{3}} x = 1$

$$x = \left(\frac{4}{3}\right)^1 \Rightarrow x = \frac{4}{3}$$

15. $\log_{100} x = -\frac{1}{2}$

$$x = 100^{-\frac{1}{2}} \Rightarrow x = \left(\frac{1}{100}\right)^{\frac{1}{2}} \Rightarrow x = \frac{1}{10}$$

16. $\log_{0,8} x = -1$

$$x = \left(\frac{8}{10}\right)^{-1} \Rightarrow x = \frac{5}{4}$$

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17. $\log (\log x) = 2$

$$\log x = 10^2 \Rightarrow x = 10^{10^2} \Rightarrow x = 10^{100}$$

18. $\log_2 (\ln (x - 1)) = 1$

$$\ln (x - 1) = 2^1 \Rightarrow x - 1 = e^2 \Rightarrow x = 1 + e^2$$

19. $\ln x = \frac{1}{2}$

$$x = e^{\frac{1}{2}} \Rightarrow x = \sqrt{e}$$

20. $\ln (x + 1) = -2$

$$x + 1 = e^{-2} \Rightarrow x + 1 = \frac{1}{e^2} \Rightarrow x = \frac{1}{e^2} - 1$$

21. $\ln (3x - 4) = 0$

$$3x - 4 = e^0 \Rightarrow 3x - 4 = 1 \Rightarrow 3x = 5 \Rightarrow x = \frac{5}{3}$$

22. $\ln x = 2 \ln 3x$

$$x = 9x^2 \Rightarrow x(9x - 1) = 0 \Rightarrow x = 0 \text{ non acc. perché } x > 0 \quad x = \frac{1}{9}$$

23. $\ln 3x + \ln \frac{x}{3} = \ln 4$

$$\text{c.a.: } x > 0: \ln \left(3x \cdot \frac{x}{3} \right) = \ln 4 \Rightarrow x^2 = 4 \Rightarrow x = \pm 2 \Rightarrow x = 2$$

24. $\ln (x + 1) = 1 + \ln 2x$

$$\text{c.a.: } \begin{cases} x + 1 > 0 \\ x > 0 \end{cases} \Rightarrow x > 0$$

$$\ln (x + 1) = \ln e + \ln 2x \Rightarrow \ln (x + 1) = \ln 2ex \Rightarrow x + 1 = 2ex$$

$$x(1 - 2e) = -1 \Rightarrow x(2e - 1) = 1 \Rightarrow x = \frac{1}{2e - 1}$$