

94.  $\log x - 1 > \frac{2}{\log x}$

Pongo:  $\log x = t \Rightarrow t - 1 - \frac{2}{t} > 0 \Rightarrow \frac{t^2 - t - 2}{t} > 0$

$-1 < t < 0 \vee t > 2 \Rightarrow \frac{1}{10} < x < 1 \vee x > 100$

$\begin{cases} \frac{1}{10} < x < 1 \vee x > 100 \\ x > 0 \end{cases} \Rightarrow \frac{1}{10} < x < 1 \vee x > 100$

95.  $\frac{\log(x-3) - 1}{1 + \log x} < 0$

$N > 0: \log(x-3) > 1 \Rightarrow x-3 > 10 \Rightarrow x > 13$

$D > 0: \log x > -1 \Rightarrow x > \frac{1}{10}$

$\begin{cases} \frac{1}{10} < x < 13 \\ x > 0 \\ x - 3 > 0 \end{cases} \Rightarrow \begin{cases} \frac{1}{10} < x < 13 \\ x > 0 \\ x > 3 \end{cases} \Rightarrow 3 < x < 13$

96.  $\log_2^2 x - 6 \log_2 x + 8 > 0$

Pongo:  $\log_2 x = t \Rightarrow t^2 - 6t + 8 > 0 \Rightarrow t_{1,2} = \frac{3 \pm \sqrt{1}}{1} = \begin{cases} 4 \\ 2 \end{cases}$

$t < 2 \vee t > 4 \Rightarrow \log_2 x < 2 \vee \log_2 x > 4$

$\begin{cases} x > 0 \\ x < 4 \vee x > 16 \end{cases} \Rightarrow 0 < x < 4 \vee x > 16$

97.  $\log_{1/4} (x^2 - 7x + 12) - \log_{1/4} (9 - x^2) > 0$

$$\log_{1/4} (x^2 - 7x + 12) > \log_{1/4} (9 - x^2)$$

$$\begin{cases} x^2 - 7x + 12 > 0 \\ 9 - x^2 > 0 \\ x^2 - 7x + 12 < 9 - x^2 \end{cases} \Rightarrow \begin{cases} x < 3 \vee x > 4 \\ -3 < x < 3 \\ 2x^2 - 7x + 3 < 0 \end{cases} \Rightarrow \begin{cases} x < 3 \vee x > 4 \\ -3 < x < 3 \\ \frac{1}{2} < x < 3 \end{cases} \Rightarrow$$

$$\frac{1}{2} < x < 3$$

98.  $\log_3^2 x - 4 \log_3 x + 3 < 0$

Pongo:  $\log_3 x = t \Rightarrow t^2 - 4t + 3 < 0 \Rightarrow 1 < t < 3 \Rightarrow$

$$1 < \log_3 x < 3 \Rightarrow 3 < x < 27$$

$$\begin{cases} 3 < x < 27 \\ x > 0 \end{cases} \Rightarrow 3 < x < 27$$