

1.  $(2a - b)^2 - (3a + b)(a - 2b) + 5a^2 - ab$   
 $= 4a^2 - 4ab + b^2 - (3a^2 - 6ab + ab - 2b^2) + 5a^2 - ab =$   
 $= 4a^2 - 4ab + b^2 - 3a^2 + 6ab - ab + 2b^2 + 5a^2 - ab = 6a^2 + 3b^2$
2.  $(x + y)^2 - 2y(x - y) - (x + y)(y - x)$   
 $= x^2 + 2xy + y^2 - 2xy + 2y^2 - (y^2 - x^2) =$   
 $= x^2 + 2xy + y^2 - 2xy + 2y^2 - y^2 + x^2 = 2x^2 + 2y^2$
3.  $(a^2 + b^2)(a^2 - b^2) - (a^2 + b^2)^2 + 2a^2(a^2 + b^2)$   
 $= a^4 - b^4 - (a^4 + 2a^2b^2 + b^4) + 2a^4 + 2a^2b^2 =$   
 $= a^4 - b^4 - a^4 - 2a^2b^2 - b^4 + 2a^4 + 2a^2b^2 = 2a^4 - 2b^4$
4.  $2(y - 3x)^2 + 2(2x + y)(y - 2x) - 9x^2 - 2xy - (2y - x)^2$   
 $= 2(y^2 - 6xy + 9x^2) + 2(y^2 - 4x^2) - 9x^2 - 2xy - (4y^2 - 4xy + x^2) =$   
 $= 2y^2 - 12xy + 18x^2 + 2y^2 - 8x^2 - 9x^2 - 2xy - 4y^2 + 4xy - x^2 = -10xy$
5.  $(x + 2)^2 - 3(x + 2)(x - 2) + (x - 2)^3 - x^2(x - 8)$   
 $= x^2 + 4x + 4 - 3(x^2 - 4) + x^3 - 6x^2 + 12x - 8 - x^3 + 8x^2 =$   
 $= x^2 + 4x + 4 - 3x^2 + 12 + x^3 - 6x^2 + 12x - 8 - x^3 + 8x^2 = 16x + 8$
6.  $x + 1 + (2x + y + 3)^2 - (2x + y)^2 - 2(3y + 5)$   
 $= x + 1 + 4x^2 + y^2 + 9 + 4xy + 12x + 6y - (4x^2 + 4xy + y^2) - 6y - 10 =$   
 $= x + 1 + 4x^2 + y^2 + 9 + 4xy + 12x + 6y - 4x^2 - 4xy - y^2 - 6y - 10 = 13x$
7.  $(a^2 + 4b^2)(2b + a)(a - 2b)(16b^4 + a^4)$   
 $= (a^2 + 4b^2)(a^2 - 4b^2)(16b^4 + a^4) = (a^4 - 16b^4)(16b^4 + a^4) = a^8 - 256b^8$
8.  $\{[x^3 - y^3 + (x + y)^3 + 2x^2y - x(2x + 3y)(x + y)]^2 - 2\}^3$   
 $= \{[x^3 - y^3 + x^3 + 3x^2y + 3xy^2 + y^3 + 2x^2y - x(2x^2 + 2xy + 3xy + 3y^2)]^2 - 2\}^3 =$   
 $= \{[2x^3 + 5x^2y + 3xy^2 - 2x^3 - 2x^2y - 3x^2y - 3xy^2]^2 - 2\}^3 = \{[0]^2 - 2\}^3 = (-2)^3 = -8$

$$\begin{aligned} 9. & [a + 3 + (b - 1)(2b + a + 3) + b(b + 2a - 1)] a - (b + a)^3 \\ & = [a + 3 + 2b^2 + ab + 3b - 2b - a - 3 + b^2 + 2ab - b] a - (a^3 + 3a^2b + 3ab^2 + b^3) = \\ & = (3b^2 + 3ab) a - a^3 - 3a^2b - 3ab^2 - b^3 = \\ & = 3ab^2 + 3a^2b - a^3 - 3a^2b - 3ab^2 - b^3 = -a^3 - b^3 \end{aligned}$$

$$\begin{aligned} 10. & \left[ (x + 3a)^2 + (2x - 3a)^2 + 4 \left( x - \frac{3}{2}a \right) (3a + x) \right] : (-3)^2 - (x - 2)^2 \\ & = \left[ x^2 + 6ax + 9a^2 + 4x^2 - 12ax + 9a^2 + 4 \left( 3ax + x^2 - \frac{9}{2}a^2 - \frac{3}{2}ax \right) \right] : 9 - (x^2 - 4x + 4) = \\ & = (x^2 + 6ax + 9a^2 + 4x^2 - 12ax + 9a^2 + 12ax + 4x^2 - 18a^2 - 6ax) : 9 - x^2 + 4x - 4 = \\ & = (9x^2) : 9 - x^2 + 4x - 4 = x^2 - x^2 + 4x - 4 = 4x - 4 \end{aligned}$$